

ΑΣΚΗΣΕΙΣ ΣΕ ΑΘΡΟΙΣΜΑ ΡΗΤΩΝ ΠΑΡΑΣΤΑΣΕΩΝ

1. $\frac{y}{x} - \frac{x+y}{x-y} + \frac{y^2}{x^2 - xy} - \frac{x(x+y)}{2y(y-x)}$ $\left(\frac{x}{2y} \right)$
2. $\frac{x^2}{a} - \frac{a^2}{x} - \frac{x^2 - 2a^2 - ax}{a+x} + \frac{(a-x)(a^2 + x^2)}{ax}$ (a)
3. $\frac{x^3 + 2x^2y - y^3}{(x+y)^3} + \frac{2y}{x+y} - \frac{xy}{x^2 + 2xy + y^2}$ (1)
4. $\frac{a+x}{a-x} + \frac{a-2x}{a+x} + \frac{a^2 + 3x^2}{x^2 - a^2}$ $\left(\frac{a}{a+x} \right)$
5. $\frac{a-2}{2a+1} + \frac{2a+1}{1-2a} - \frac{2-3a(2a+3)}{4a^2-1}$ (1)
6. $\frac{4}{a^2 - x^2} + \frac{3x}{a^2x - a^3} - \frac{a-3x}{a^3 - ax^2}$ $\left(\frac{3}{a^2} \right)$
7. $\frac{2(a-x)}{a^3 + a^2x} + \frac{a+x}{a^3 + ax^2 + 2a^2x} - \frac{5}{a^2 + ax}$ $\left(-\frac{2}{a^2} \right)$
8. $\frac{a-3}{3a^2+a} - \frac{a+3}{a-3a^2} - \frac{a}{9a^2-1} + \frac{4a^2-7}{9a^3-a}$ $\left(\frac{1}{a} \right)$
9. $\frac{x+2}{x^2 + 7x + 10} - \frac{x-3}{x^2 - 8x + 15} + \frac{x^2 - 15}{x^2 - 25}$ (1)
10. $\frac{2x+1}{x^2 - 5x + 6} - \frac{x+3}{x^2 - x - 6} - \frac{x+5}{x^2 - 4} - \frac{19}{x^3 - 3x^2 - 4x + 12}$ $\left(\frac{2}{(x-2)(x-3)} \right)$
11. $\frac{x^2}{2a^2 + 2ax} - \frac{a^2}{3ax + 3x^2} + \frac{a^2 - 2x^2}{3ax} - \frac{1}{2} + \frac{a+6x}{6a+6x}$ $\left(-\frac{x}{6a} \right)$
12. $\frac{a+3}{a-2} - \frac{a+1}{a-1} - \frac{2a+1}{a^2 - 3a + 2}$ $\left(\frac{1}{a-1} \right)$
13. $\frac{x}{x^2 - 1} + \frac{x^2 + x + 1}{x^3 - x^2 + x - 1} - \frac{x^2 - x - 1}{x^3 + x^2 + x + 1} + \frac{4x^2 + 3x}{1 - x^4}$ $\left(\frac{x^3}{x^4 - 1} \right)$
14. $\frac{2x-4}{x^2 - 4x + 3} - \frac{x+1}{x^2 - x - 6} - \frac{x+3}{x^2 + x - 2} - \frac{x^2 - x - 4}{(1-x)(2+x)(x+3)}$ $\left(\frac{1}{x^2 + 4x + 3} \right)$
15. $\frac{1}{a^3 - a^2x - a^2y + axy} + \frac{1}{y^3 - y^2x - ay^2 + axy} + \frac{1}{x^3 - yx^2 - ax^2 + axy}$ $\left(\frac{1}{axy} \right)$

Οι παραστάσεις μέσα στις παρενθέσεις δεξιά, είναι τα αποτελέσματα που πρέπει να βρείτε.